[Suppressing quantum errors by scaling a surface code logical qubit](https://www.nature.com/articles/s41586-022-05434-1)

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 The circuits were benchmarked in simultaneous operation using random circuit techniques, on the 49 qubits used in distance-5 and the 4 CZ layers from the stabilizer circuit

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 we implement single-qubit rotations, controlled-Z (CZ) gates, reset and measurement, demonstrating similar or improved simultaneous performance

 We attribute this rise to data qubits leaking into non-computational excited states and anticipate that the inclusion of leakage-removal techniques on data qubits would help to mitigate this rise

 we compute an appropriately normalized correlation pij between detection events occurring on any two detectors i and j

We use a generalization of pij to determine these probabilities

 To understand the contributions of individual components to our logical error performance, we follow

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